LETTERS TO THE EDITOR

Crystal Structure of β -VO(HPO₄) · 2H₂O Solved from X-Ray Powder Diffraction

A LE BAIL AND G. FEREY

Laboratoire des Fluorures, UA CNRS 449, Faculté des Sciences, Université du Maine, Route de Laval, 72017 Le Mans Cedex, France

P. AMOROS AND D. BELTRAN-PORTER

Departament de Quimica Inorganica, Facultat de Ciencies Quimiques, Universitat de Valencia, Dr Moliner 50, 46100 Burjassot, Valencia, Spain

AND G. VILLENEUVE

Laboratoire de Chimie du Solide du CNRS, Université de Bordeaux I, 351 Cours de la Libération, 33405 Talence Cedex, France

Communicated by J. M. Honig, November 3, 1988

The crystal structure of β -VO(HPO₄) \cdot 2H₂O has been determined from X-ray powder diffraction data. The cell is triclinic (space group PI, Z = 4) with a = 5.659(2) Å, b = 7.578(4) Å, c = 12.623(5) Å, $\alpha = 89.66(2)^\circ$, $\beta = 102.14(2)^\circ$, and $\gamma = 92.23(2)^\circ$. Starting positional parameters were obtained by direct methods applied to 640 reflections which are derived from a modified Rietveld analysis working without structural model. The structure was refined using Rietveld profile refinement principles. The final reliability factors were $R_1 = 0.039$, $R_p = 0.076$, and $R_{wp} = 0.092$. The structure is built up of chains of corner-shared VO₄(H₂O)₂ octahedra and (HPO₄) tetrahedra alternated along the c crystallographic axis. These chains are interconnected through HPO₄ groups forming layers stacked in the [100] direction. In contrast to α -VO(HPO₄) \cdot 2H₂O, there are no isolated water molecules between the layers. © 1989 Academic Press, Inc.

Introduction

The oxovanadium(V) phosphate dihydrate can be considered as a chemical precursor of a wide family of oxovanadium(IV) or (V) derivatives (1-4). Among them, several oxovanadium(IV) compounds having the general stoichiometry VO(H_xPO₄)_x · nH₂O have been studied in detail owing to their catalytic relevance (5, 6). The oxovanadium(IV) hydrogenphosphates, which can be considered derivatives of the VOPO₄ \cdot 2H₂O obtained by redox intercalation of protons (7), are the most widely used precursors of the active phase for *n*butane oxidation.

These materials display a large variety of crystal structures owing to the great number of possible connectivity patterns among VO_6 octahedra and PO_4 tetrahedra (8-13).

Such a diversity of patterns results in a wide set of vanadium-vanadium bridging modes suitable to support magnetic interactions (14, 15).

The synthesis of some new oxovanadium(IV) hydrogenphosphates has been recently reported (7). It seems clear that the knowledge of their crystal structures would allow one to clarify both the catalytic activity of the vanadium-phosphate system and the relationship between the magnetic behavior and the topology of the bridges in the VO₆-PO₄ entities.

The application of new powder diffraction methodologies when single crystals are not available, as occurs with β -VO(HPO₄) · 2H₂O, has now proved its capacity for crystal structure determination. The structures of several phosphates, including that of α -VO(HPO₄) · 2H₂O (*12*), have been recently solved in this way (*16*). We present here the full crystal structure determination of another form of the latter compound, β -VO(HPO₄) · 2H₂O, from its X-ray powder pattern. It is to be noted that a wrong formulation was previously proposed for this material, i.e., VO(HPO₄) · 1.5H₂O (*3*).

Experimental

Sample preparation. We described elsewhere the synthetic strategy of all $VO(HPO_4) \cdot nH_2O$ known compounds (3, 7). The obtention of a given phase depends drastically on the solvent composition and on the reaction time.

The β -VO(HPO₄) · 2H₂O was prepared by heating to reflux (at 50°C) for 50 hr a mixture of 4.17 g of V₂O₅, 24 cm³ of H₃PO₄ 85%, and 4 cm³ of Hl 57% in an acetone water mixture in the ratio 27:1. The reaction time of the process may be reduced to 24 hr by using a lower acetone-water ratio (ca. 16). However, in this case, a more prolonged reflux time leads to the α -VO(HPO₄) · 2H₂O phase (7, 12).

Data collection. The powder diffraction

pattern was scanned in steps of 0.02° (2 θ) over the angular range $10-95^{\circ}(2\theta)$ during 35 sec per step, using a Siemens D 501 diffractometer. The $CuK\alpha$ radiation was selected by a graphite monochromator in the reflected beam. In order to minimize the orientation effects, the sample holder described by MacMurdie et al. (17) was used. impurities detected: Two were α- $VO(HPO_4) \cdot 2H_2O$ and $VO(HPO_4) \cdot 4H_2O$; the integrated intensities of the most intense reflections of these phases were less than 1% that of the major phase.

Data Analysis

Indexing was realized using the program TREOR (18). The most probable solution was triclinic. After reduction of the cell to a pseudomonoclinic one, the refined parameters were a = 5.660(3) Å, b = 7.578(4) Å, c = 12.623(5) Å, $\alpha = 89.66(2)^{\circ}$, $\beta = 102.14(2)^{\circ}$, and $\gamma = 92.23(2)^{\circ}$. The calculated density for Z = 4 was 2.50 g cm⁻³.

In order to obtain the maximum number of individual intensities, the profile fitting procedure with cell constraints described in (19) was applied. When possible, excluded zones were used in order to eliminate some contributions of the two impurities. The refinement without structural model, already described elsewhere (12), led to the conventional Rietveld profile reliability factors $R_{\rm p} = 7.5\%$ and $R_{\rm wp} = 9.4\%$ for 967 reflections up to 95° (2 θ). Intensities were then converted into structure factors and used as input data for the SHELX program (20). Atomic scattering factors and anomalous dispersion correction were obtained from the "International Tables for X-ray Crystallography" (21). The application of the automatic centrosymmetric direct fast methods facilities of the SHELX76 program, using the 640 first reflections of the powder pattern, gave a first set of coordinates of 2 vanadium, 2 phosphorus, and 10 oxygen atoms. A new profile Rietveld re-

Lattice constants	a (Å), 5.659(2),	b (Å) 7.578(4),	c (Å) 12.623(5),	α (°), 89.66(2),	β (°), 102,14(2).	γ (°) 92.23(2).	
Volume (Å ³)		528.86			102/1 (2),	, _ (2),	
Density (g cm ⁻³)		2.50					
Space group		PĨ					
2θ range (°)		10-95					
Step scan increment (2θ)		0.02					
No. of reflections		967					
No. of structural p	arameters	54					
Profile parameters	(definition i	n (19)):					
$U_1 = 0.79(4),$		$V_1 = -0.53(3),$		W_1	$W_1 = 0.258(6)$		
$U_2 = 0,$		$V_2=0,$		W_2	$W_2 = 1.204(9)$		
C = 0.0	082(2),	D =	-0.427(7)				
Zero point (2θ)	0.068(2)						
Reliability factors ((%)	$R_1=3.89,$	$R_{\rm p} = 7.6$	$4, \qquad R_{\rm wp} =$	9.18, R _E	= 2.39	

TABLE I Details of Rietveld Refinement

finement using this set of atomic positions as structural model, followed by Fourier difference syntheses, yielded the position of the remaining oxygen atoms. Hydrogen atoms were not detected. Details of the final refinements are given in Table I and final atomic coordinates of nonhydrogen at-

TABLE II Positional and Thermal Parameters for β -VO(HPO₄) \cdot 2H₂O

Atom	x/a	y/b	z/c	β (Ų)	
V(1)	0.8860(7)	0.2762(5)	0.3628(3)	0.38(4)	
V(2)	0.9087(7)	0.2197(5)	0.8621(3)	0.38(4)	
P(1)	0.831(1)	0.3440(8)	0.6101(5)	1.66(9)	
P(2)	0.847(1)	0.1605(7)	0.1070(5)	1.66(9)	
O(1)	0.963(2)	0.269(1)	0.713(1)	2.74(9)	
O(2)	0.958(2)	0.267(1)	0.219(1)	2.74(9)	
O(3)	0.959(2)	0.237(1)	0.023(1)	2.74(9)	
O(4)	0.882(2)	0.229(1)	0.509(1)	2.74(9)	
O(5)	0.265(2)	0.382(1)	0.903(1)	2.74(9)	
O(6)	0.224(2)	0.112(1)	0.406(1)	2.74(9)	
O(7)	0.860(2)	0.543(2)	0.5976(9)	2.74(9)	
O(8)	0.858(2)	0.962(2)	0.1211(9)	2.74(9)	
O(9)	0.646(2)	0.400(1)	0.3312(8)	2.74(9)	
O(10)	0.671(2)	0.099(1)	0.8364(9)	2.74(9)	
O(11)	0.550(2)	0.3136(9)	0.603(1)	2.74(9)	
O(12)	0.548(2)	0.197(1)	0.0805(9)	2.74(9)	
O(13)	0.726(2)	0.019(1)	0.3417(9)	2.74(9)	
O(14)	0.765(2)	0.466(1)	0.860(1)	2.74(9)	

oms in Table II. Figure 1 shows the observed and calculated patterns.

Description of the Structure

Projections of the structure along the [100] and [010] directions are shown in Figs. 2 and 3. The crystal structure consists of vanadyl hydrogen phosphate layers stacked along the *a* axis and held together by hydrogen bonding. Contrary to the α -VO(HPO₄) \cdot 2H₂O (*12*), there is no isolated water molecules between the layers. The layer organization may be described in two ways:

--Chains of alternating VO₆ octahedra and PO₄ tetrahedra sharing corners and running along the *c* direction. In each chain, both the apical hydroxyl oxygen of the HPO₄ groups and the oxygen of the VO²⁺ groups are pointing toward the same adjacent layer. This direction is just the opposite in the neighboring chains. The HPO₄ groups in a chain are alternatively connected to the two neighboring chains in the *b* direction. This network generates two kinds of rings in the layer: a classical tetrameric small one built up from two VO₆ octahedra *cis*-connected through two PO₄ tetra-



FIG. 1. Observed (...) and calculated (...) patterns of β -VO(HPO₄) · 2H₂O. The difference pattern is at the same scale.

hedra, and a larger one elongated in the c direction and formed by four VO₆ octahedra interconnected through PO₄ tetrahedra. This way, piling up of the layers gives rise to channels along the a axis.



FIG. 2. Projection of the structure of β -VO(HPO₄) · 2H₂O along [100].

—Two nearly identical but independent units of two octahedra share corners with two tetrahedra related by the centers of inversion of the cell. These units share four corners with four other similar units. One can note that the two independent units are *quasi*-related by the symmetry operation x, 1/2 - y, 1/2 + z. So, if the α and γ angles



FIG. 3. Projection of the structure of β -VO(HPO₄) - 2H₂O along [010].

were 90° the space group would be $P2_1/c$. The atomic coordinates in Table II are arranged in order to demonstrate this fact, which justifies the final choice of the cell. Refinement attempted with the strict constraint cited above led to $R_1 = 7\%$ instead of 3% for the real cell.

At this stage of the description, a valence bond analysis (VBA) using Brown's data (22, 24) provides a better understanding of the structure (Table IV) concerning the details of the cationic coordination, the location of OH groups and H₂O molecules, and the hydrogen bonds. Indeed, for the last two points, it must be recalled (22) that in H₂O molecules or OH ions, the O-H bond strength corresponds approximately to 0.8 valence unit. Therefore, if the oxygen of OH or H₂O is also bonded to one (or several) cations (including H of another water molecule, which can give 1 - 0.8 = 0.2v.u.), it must receive from this cation 2.0 -0.8 = 1.2 v.u. (if OH) or 2.0 - (2 * 0.8) =0.4 v.u. (if H₂O) to complete its base strength to 2.0. The difference between 2.0 and the calculated bond valence of oxygen gives information on the nature of the ligands around V and P, and on the oxygens involved in hydrogen bonding.

The vanadium atoms are coordinated in a $pseudo-C_{4v}$ distorted octahedral environment (really C_1). Both V(1) and V(2) atoms show a short V–O distance (d(V(1)-O(9)))= 1.66 Å, and d(V(2)-O(10)) = 1.57 Å) corresponding to the double bond of the oxovanadium(IV) group. The first water molecule of these octahedral, corresponding to O6 and O5 for V1 and V2, respectively, is in *trans* position to the double bond (d(V - OH_2 = 2.3 Å) and weakly bonded to vanadium (0.2 v.u.). Therefore, it may be expected that O-H bonds within this type of water molecule will be shorter (0.90 Å) than the common O-H distance (0.96 Å). The equatorial plane of the VO6 octahedra is defined by the four remaining oxygen atoms.

Three of them link the octahedra to hydrogenphosphate groups and the fourth, pointing alternatively to the positive and negative sense of the b axis along each chain, corresponds to a water molecule as it appears for O13 and O14 in the VBA analysis of Table IV. These water molecules are normally bounded to vanadium atoms (0.40 v.u.); this precludes normal O-H bond lengths in this H₂O molecule (0.90–0.93 Å). This kind of polyhedron, very similar to that observed in VO(HPO₄) \cdot 4H₂O (9), is characteristic of oxovanadium(IV) in other phosphate systems. One must note however the slight difference between V1 and V2 octahedra concerning the double bond. Whereas V(2)–O(10) (bond length 1.57 Å) completely saturates the base strength of O10, it is not the case for V(1)-O(9) (1.66) Å) for which 0.5 v.u. are available on O9 for further weak hydrogen bonding.

From Table III, it is clear that the PO₄

TABLE III

Selected Interatomic Distances (Å) and Angles (°) in β -VO(HPO₄) · 2H₂O

VO ₆ groups					
1.66(1)	V(2)-O(10)	1.57(1)			
1.88(1)	V(2)-O(8)	1.93(1)			
1.94(1)	V(2)-O(3)	1.99(1)			
1.95(1)	V(2)-O(1)	2.01(2)			
2.11(1)	V(2)-O(14)	2.06(1)			
2.29(1)	V(2)-O(5)	2.29(1)			
99.7(9)	O(10)-V(2)-O(8)	98.6(9)			
100.3(9)	O(10)-V(2)-O(3)	100.3(9)			
97.2(9)	O(10)-V(2)-O(1)	101.2(9)			
101.7(9)	O(10)-V(2)-O(14)	100.8(9)			
178.4(9)	O(10)-V(2)-O(5)	176(1)			
91.9(9)	O(8)-V(2)-O(3)	89.3(9)			
162.7(9)	O(8)-V(2)-O(1)	89.9(9)			
82.2(9)	O(8)-V(2)-O(14)	160.5(9)			
PO ₄	groups				
1.47(1)	P(2)O(3)	1.46(2)			
1.52(1)	P(2)-O(8)	1.52(1)			
1.58(1)	P(2)-O(2)	1.63(1)			
1.63(1)	P(2)-O(12)	1.58(1)			
116.1(9)	O(3)-P(2)-O(8)	116.5(9)			
108(1)	O(3)-P(2)-O(2)	107.6(9)			
109(1)	O(3)-P(2)-O(12)	110.5(9)			
103(1)	O(8)-P(2)-O(2)	112.5(9)			
114.5(9)	O(8)-P(2)-O(12)	104(1)			
103.9(9)	O(2)-P(2)-O(12)	105(1)			
	VO6 1 1.66(1) 1.88(1) 1.94(1) 1.95(1) 2.11(1) 2.29(1) 99.7(9) 100.3(9) 97.2(9) 101.7(9) 178.4(9) 91.9(9) 162.7(9) 82.2(9) PO4 1 1.47(1) 1.52(1) 1.58(1) 1.63(1) 116.1(9) 108(1) 109(1) 103(1) 114.5(9) 103.9(9)	$\begin{array}{llllllllllllllllllllllllllllllllllll$			

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Valance Bond Analysis of β -VO(HPO4) \cdot 2H2O Using the Zachariasen Law (23)						
	V (1)	V(2)	P(1)	P(2)	$\Sigma (\Sigma_{exp} = 2)$	Comments
O(1)		2.01(1)	1.47(1)			s
		0.50(2)	1.51(4)		2.01	
O(2)	1.95(1)			1.63(1)		h.b.
	0.60(2)			0.97(3)	<u>1.57</u>	
O(3)		1.99(1)		1.46(1)		s
		0.53(2)		<u>1.56(3)</u>	2.09	
O(4)	1.88(1)		1.63(1)			h.b.
	0.75(3)		<u>0.97(3)</u>		1.72	
O(5)		2.29(1)				w
		0.20(1)			0.20	
O(6)	2.29(1)					w
	0.20(1)				0.20	
O(7)	1.94(1)		1.52(1)			8
	0.62(2)		1.32(4)		1.97	
O(8)		1.93(1)		1.52(1)		s
		0.65(2)		1.32(4)	1.94	
O(9)	1.66(1)					h.b.
	1.50(5)				1.50	
O(10)		1.57(1)			_	s
```		1.99(2)			1.99	
<b>O</b> (11)			1.58(1)			hy
			1.11(4)		1.11	-
O(12)				1.58(1)		hy
~ (1~)				1.11(4)	1.11	2
O(13)	2.11(1)					w
	0.36(2)				0.36	
O(14)		2.06(1)				w
-()		0.43(2)			0.43	
Σ	4.03	4.30	4.91	4.96		
Σexpected	4	4	5	5		
-capecied	•	-	-	-		

TABLE IV

Note.  $s = \exp[(R_0 - R)/B)]$  with  $R_0 = 1.62$ , B = 0.36 for P and  $R_0 = 1.79$ , B = 0.319 for V. In each case of this table, the first line corresponds to the distance (Å) and the second line to the bond strength in valence units (underlined).

a s, saturated; h.b., hydrogen bonding on the concerned atom; hy, the oxygen corresponds to the OH group bonded to P; w, the oxygen corresponds to a water molecule.

tetrahedra are slightly distorted, as in other oxovanadium(IV) phosphates (9, 12, 13). Obviously (Table IV), O11 and O12 apical oxygens correspond to the O-H group of the hydrogenphosphate. As 0.90 v.u. are missing to these oxygens, they would be provided by H at R = 0.91 Å, using the power law  $s_{\rm H} = (R/R_0)^{-N}$  with  $R_0 = 0.87$  Å and N = 2.2 (24). Finally, the intra- and interlayer hydrogen bonding involves O2, O4, O5, O6, O9, O11–O14, as indicated in Table IV. The hydrogen bond framework involves very likely PO–H…O=V and *trans*-OH₂–(OH)P networks. In any case the hydrogen bonds would be weak, as predicted from the analysis of the IR spectrum of this compound (7).

In a recent work (7), it has been proposed that the known monohydrogenphosphate phases can be classified in three different structural types, namely Type I, VO(HPO₄)  $\cdot$  0.5H₂O; Type II,  $\alpha$ -VO(HPO₄)  $\cdot$  2H₂O; Type III, VO(HPO₄)  $\cdot$  4H₂O and  $\beta$ -VO(HPO₄)  $\cdot$  2H₂O. Particularly, the  $\beta$ -dihydrate appears as intermediate in the thermal treatment of the tetrahydrate from both thermogravimetric and thermodiffractometric experiments. Moreover, the structure of  $\beta$ -VO(HPO₄) · 2H₂O is closely related with that of  $VO(HPO_4) \cdot 4H_2O$  (9). Both compounds present a similar arrangement of VO₆ octahedra and PO₄ tetrahedra forming alternating chains which lie along the c direction in the  $\beta$ -dihydrate and along the a direction in the tetrahydrate (Fig. 4). The coordination geometry around both vana-



FIG. 4. View of the infinite double chains of VO₆ octahedra and PO₄ tetrahedra running along the [100] direction in VO(HPO₄)  $\cdot$  4H₂O.

dium and phosphorus atoms is similar in both structures. Each phosphate group contains three oxygen atoms (shared with three different vanadium atoms) and a hydroxyl group. The vanadium atoms show very similar coordination polyhedra, having a water molecule trans-coordinated to the axial V=0 group and a second coordinated water molecule in the equatorial plane of the  $VO_6$  octahedra. The similarity of these structures suggests that the dehydration of the tetrahydrate into the dihydrate may proceed topotactically. However, several ways for the reorganization of the infinite double chains that lie parallel to the *a* axis (6.379 Å) of the tetrahydrate may be imagined to give the interconnected single chains running in the c direction (12.623) Å = 2 * 6.379 Å) of the  $\beta$ -dihydrate. All the possible models that we imagined need to break some bonds (at least two or four per unit cell), to rotate some polyhedra, and to reconstruct the bonds. Only a careful study of the orientational relation (if any) between the two phases when dehydrating a single crystal of the tetrahydrate could give us some arguments, but fragmentation of the crystal will probably occur, owing to the large volume variation. A neutron thermodiffractometric (powder) experiment is planned at ILL, which could also be informative.

#### Conclusion

An interesting feature concerning the crystal structures of all the known oxovanadium(IV) phosphates is the presence of a simple structural unit built up of two VO₆ octahedra *cis*-bridged through two  $\mu$ (OO')-phosphate tetrahedra (3). Both the inner topology of these tetrameric units and the nature of their connectivity are characteristic for each crystalline phase. Thus, the degree of coplanarity of the equatorial planes of the VO₆ octahedra, the possible existence of an inversion center, and the relative orientation of the HPO₄ and VO₆ units are significant as topological parameters. On the other hand, there exists a correlation between the connectivity and the hydration degree. In fact, the number of connections between the tetrameric units decreases as the hydration degree increases (12 for the (VO)₂P₂O₇, 8 or 10 for the VO(HPO₄)  $\cdot$  0.5H₂O, 8 for the  $\alpha$ -VO(HPO₄)  $\cdot$  2H₂O, and 4 for  $\beta$ -VO(HPO₄)  $\cdot$  2H₂O and VO(HPO₄)  $\cdot$  4H₂O). A detailed crystal-chemistry comparative analysis of all these structures will be published later.

#### Acknowledgments

This work was supported by the EEC under Grant ST 2J-0164-4-E(CD). P.A. thanks the Spanish Ministerio de Educación y Ciencia for a FPI fellowship.

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